

**QUESTION 1**

**Shortest Paths**

**(6+1 = 7 points)**

**Apply the Dijkstra Algorithm for finding the shortest distances from S to A..G**

Distances

SA = 3.2    SB = 5.1    SC = 3.6  
 CG = 7.8    EG = 5.7    DG = 5.1  
 AB = 2.0    BD = 2.8    DE = 3.2  
 EC = 2.2    CA = 2.2

Ready Set = _____							
<b>Node</b>	<b>Start</b>	<b>A</b>	<b>B</b>	<b>C</b>	<b>D</b>	<b>E</b>	<b>Goal</b>
Distance	0						
Predecessor	-						
Shortest Distance S-->G _____							
Shortest Path S--> G: _____							

**QUESTION 2**                      *Maze Navigation*

**(4 points)**

**Consider this iterative algorithm:**

```
while(1)
{ if (right_open) VWTurn(-90,100) VWWait();           // turn right
  else if (front_open) ;                               // no turn
  else if (left_open) VWTurn(90,100) VWWait();        // turn left
  else VWTurn(180,100) VWWait();                      // turn 180
  VWStraight(100,100); VWWait();}                     // go 1 cell
```

**In which order will the robot visit the maze cells?**



**Consider this recursive algorithm:**

```
void explore()
{ "mark current cell";
{ if (front_open && "front cell unmarked")
  { "drive 1 cell forward"; explore(); "drive 1 cell back"; }
if (left_open && "left cell unmarked")
  { "drive 1 cell left"; explore(); "drive 1 cell right"; }
if (right_open && "right cell unmarked")
  { "drive 1 cell right" explore(); "drive 1 cell left"; }
}
```

**In which order will the robot visit the maze cells?**



**QUESTION 3**

*Waypoint Navigation*

**(10 points)**

**Write a C-function `drive_waypoint` that drives a mobile robot from its current position to the next waypoint, with absolute position: `wx`, `wy`.**

- You can assume that there will be a collision-free path to the waypoint.
- Continually read the robot's current pose using functions **`VWGetPosition(&x,&y,&phi)`**.

```
void drive_waypoint(float wx, float wy)
{
```

**QUESTION 4**

*Genetic Algorithms*

**(6 points)**

**Write Pseudocode to describe a Genetic Algorithm, to evolve a robot movement.**

- Assume the robot movement can be coded by 50 integers: **int move[50]**
- Use a population of 1,000 genes: **int genepool[1000][50]**
- Use an array of fitness values: **int fitness[1000]**
- Assume an evaluation function exists to assign a fitness value to each movement:  
**int eval( int robmove[])**
- Assume you have functions available.  
**void crossover(int parent1[], int parent2[], int child1[], int child2[]);**  
**void mutation(robmove[]);**  
**int select(fit[]);**

**QUESTION 5**

***Differential-Kinematics***

**(2+2 = 4 points)**

**For a differential drive vehicle with:**

- Wheel radius 4cm
- Left/right wheels are 15cm apart

**(a) Forward**

**Calculate  $v$  and  $\omega$  for**

$$\theta'_L = 2.2 \text{ rev/s}$$

$$\theta'_R = 1.5 \text{ rev/s}$$

$$v = \underline{\hspace{2cm}} \text{ m/s} \quad \omega = \underline{\hspace{2cm}} \text{ rad/s}$$

**(b) Inverse**

**Calculate  $\theta_L$  and  $\theta_R$  for:**

- $v = 1.5 \text{ m/s}$
- $\omega = -45 \text{ deg/s}$  (*careful with units!*)

$$\theta'_L = \underline{\hspace{2cm}} \text{ rev/s} \quad \theta'_R = \underline{\hspace{2cm}} \text{ rev/s}$$

**QUESTION 6**

***Ackermann-Kinematics***

**(2+2 = 4 points)**

**For an Ackermann-steering vehicle:**

- Assume wheel radius is 4cm
- Front/back wheels are 20cm apart

**(a) Forward**

Calculate the resulting angular velocity.

- $v = 1 \text{ m/s}$
- Steering angle  $10^\circ$

$\omega =$  \_\_\_\_\_ rad/s

**(b) Inverse**

What steering angle is required for a desired angular velocity.

- $\omega = 2 \text{ rad/s}$
- $v = 2 \text{ m/s}$

$\alpha =$  \_\_\_\_\_ deg

**QUESTION 7**

**Omni-Kinematics**

**(2+2+2+2 = 8 points)**

**For an omni-directional vehicle with 4 driven Mecanum wheels:**

- Assume wheel radius is 4cm
- Left/right wheels are 15cm apart
- Front/back wheels are 20cm apart

**Forward**

What is the resulting speed for individual wheel speeds:

(a)  $\dot{\Theta}_{FL} = 360^\circ/s$     $\dot{\Theta}_{FR} = -360^\circ/s$     $\dot{\Theta}_{BL} = -360^\circ/s$     $\dot{\Theta}_{BR} = 360^\circ/s$

$v_x =$                        $v_y =$                        $\omega =$

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(b)  $\dot{\Theta}_{FL} = 180^\circ/s$     $\dot{\Theta}_{FR} = 180^\circ/s$     $\dot{\Theta}_{BL} = 180^\circ/s$     $\dot{\Theta}_{BR} = 180^\circ/s$

$v_x =$                        $v_y =$                        $\omega =$

---

**Inverse**

Calculate the four individual wheel speeds in  $^\circ/s$  for desired vehicle speeds:

(c)  $v_x = 1\text{m/s}$ ,  $v_y = 1\text{m/s}$ ,  $\omega = 0$

$\dot{\Theta}_{FL} =$                $\dot{\Theta}_{FR} =$                $\dot{\Theta}_{BL} =$                $\dot{\Theta}_{BR} =$

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(d)  $v_x = 2\text{m/s}$ ,  $v_y = 0\text{m/s}$ ,  $\omega = 30^\circ/s$

$\dot{\Theta}_{FL} =$                $\dot{\Theta}_{FR} =$                $\dot{\Theta}_{BL} =$                $\dot{\Theta}_{BR} =$

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