

(a) $F = \overline{XZ} + XYZ$

| X | Y | Z | \overline{XZ} | XYZ | F |
|---|---|---|-----------------|-------|---|
| 0 | 0 | 0 | 1 | 0 | 1 |
| 0 | 0 | 1 | 0 | 0 | 0 |
| 0 | 1 | 0 | 1 | 0 | 1 |
| 0 | 1 | 1 | 0 | 0 | 0 |
| 1 | 0 | 0 | 0 | 0 | 0 |
| 1 | 0 | 1 | 0 | 0 | 0 |
| 1 | 1 | 0 | 0 | 0 | 0 |
| 1 | 1 | 1 | 0 | 1 | 1 |

(b) $G = \overline{X} + X\overline{Y}Z + Y\overline{Z}$

| X | Y | Z | $X\overline{Y}Z$ | $Y\overline{Z}$ | G |
|---|---|---|------------------|-----------------|---|
| 0 | 0 | 0 | 0 | 0 | 1 |
| 0 | 0 | 1 | 0 | 0 | 1 |
| 0 | 1 | 0 | 0 | 1 | 1 |
| 0 | 1 | 1 | 0 | 0 | 1 |
| 1 | 0 | 0 | 0 | 0 | 0 |
| 1 | 0 | 1 | 1 | 0 | 1 |
| 1 | 1 | 0 | 0 | 1 | 1 |
| 1 | 1 | 1 | 0 | 0 | 0 |

Q. 5

(a)

$$F = XYZ + \bar{X}Y$$

| X | Y | Z | XYZ | $\bar{X}Y$ | F |
|---|---|---|-----|------------|---|
| 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 0 | 0 | 0 |
| 0 | 1 | 0 | 0 | 1 | 1 |
| 0 | 1 | 1 | 0 | 1 | 1 |
| 1 | 0 | 0 | 0 | 0 | 0 |
| 1 | 0 | 1 | 0 | 0 | 0 |
| 1 | 1 | 0 | 0 | 0 | 0 |
| 1 | 1 | 1 | 1 | 0 | 1 |

(b)

$$F = \overline{(XYZ)} \overline{(\bar{X}Y)}$$

| X | Y | Z | \overline{XYZ} | $\overline{\bar{X}Y}$ | F |
|---|---|---|------------------|-----------------------|---|
| 0 | 0 | 0 | 1 | 1 | 0 |
| 0 | 0 | 1 | 1 | 1 | 0 |
| 0 | 1 | 0 | 1 | 0 | 1 |
| 0 | 1 | 1 | 1 | 0 | 1 |
| 1 | 0 | 0 | 1 | 1 | 0 |
| 1 | 0 | 1 | 1 | 1 | 0 |
| 1 | 1 | 0 | 1 | 1 | 0 |
| 1 | 1 | 1 | 0 | 1 | 1 |

(c)

The two circuits are equivalent

Q6

$$\bar{F} = \bar{B}D + \bar{A}B\bar{C} + ACD + \bar{A}BC$$

$$F = \overline{(\bar{B}D + \bar{A}B\bar{C} + ACD + \bar{A}BC)}$$

$$= \overline{(\bar{B}D + \bar{A}B(\bar{C} + C) + ACD)}$$

$$= \overline{(\bar{B}D + \bar{A}B + ACD)}$$

$$= (B + \bar{D})(A + \bar{B})(\bar{A} + \bar{C} + \bar{D})$$

$$= (AB + A\bar{D} + \cancel{B\bar{B}} + \bar{B}\bar{D})(\bar{A} + \bar{C} + \bar{D})$$

$$= \bar{A}\bar{B}\bar{D} + AB\bar{C} + A\bar{C}\bar{D} + \bar{B}\bar{C}\bar{D}$$

$$+ AB\bar{D} + A\bar{D} + \bar{B}\bar{D}$$

$$= \bar{B}\bar{D} \left[\cancel{1 + \bar{A} + \bar{C}} \right] + A\bar{D} \left[\cancel{1 + \bar{C} + B} \right]$$

$$+ AB\bar{C}$$

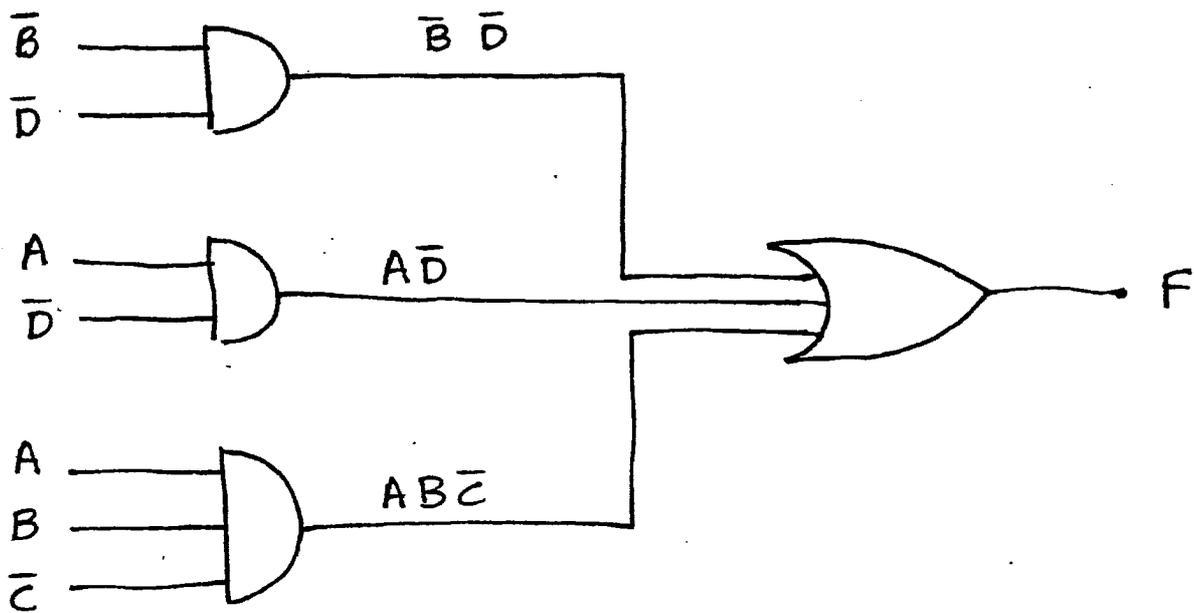
$$F = \bar{B}\bar{D} + A\bar{D} + AB\bar{C}$$

Q7.

| A | B | C | D | $\bar{B}D$ | $\bar{A}B\bar{C}$ | ACD | $\bar{A}BC$ | \bar{F} | F |
|---|---|---|---|------------|-------------------|-----|-------------|-----------|---|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 1 | 0 |
| 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1 | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |

| A | B | C | D | $\bar{B}\bar{D}$ | $A\bar{D}$ | $AB\bar{C}$ | | F |
|---|---|---|---|------------------|------------|-------------|--|---|
| 0 | 0 | 0 | 0 | 1 | 0 | 0 | | 0 |
| 0 | 0 | 0 | 1 | 1 | 0 | 0 | | 0 |
| 0 | 0 | 1 | 0 | 0 | 0 | 0 | | 0 |
| 0 | 0 | 1 | 1 | 0 | 0 | 0 | | 0 |
| 0 | 1 | 0 | 0 | 0 | 0 | 0 | | 0 |
| 0 | 1 | 0 | 1 | 0 | 0 | 0 | | 0 |
| 0 | 1 | 1 | 0 | 0 | 0 | 0 | | 0 |
| 0 | 1 | 1 | 1 | 0 | 0 | 0 | | 0 |
| 1 | 0 | 0 | 0 | 1 | 0 | 0 | | 0 |
| 1 | 0 | 0 | 1 | 1 | 0 | 0 | | 0 |
| 1 | 0 | 1 | 0 | 0 | 0 | 0 | | 0 |
| 1 | 0 | 1 | 1 | 0 | 0 | 0 | | 0 |
| 1 | 1 | 0 | 0 | 0 | 0 | 0 | | 0 |
| 1 | 1 | 0 | 1 | 0 | 0 | 0 | | 0 |
| 1 | 1 | 1 | 0 | 0 | 0 | 0 | | 0 |
| 1 | 1 | 1 | 1 | 0 | 0 | 0 | | 0 |

Q8



$$\begin{aligned}
\text{Q9. (a)} \quad & ABC + \bar{A}\bar{B}C + \bar{A}BC + AB\bar{C} + \bar{A}\bar{B}\bar{C} \\
&= BC(\cancel{A+\bar{A}}) + \bar{A}\bar{B}(\cancel{C+\bar{C}}) + AB\bar{C} \\
&= BC + \bar{A}\bar{B} + AB\bar{C} \\
&= B(C + A\bar{C}) + \bar{A}\bar{B} \\
&= B(C + A)(\cancel{C+\bar{C}}) + \bar{A}\bar{B} \\
&= B(A + C) + \bar{A}\bar{B}
\end{aligned}$$

$$\begin{aligned}
\text{(b)} \quad & \overline{(\bar{C}\bar{D}) + A} + A + CD + AB \\
&= CD\bar{A} + A + CD + AB \\
&= CD(\cancel{\bar{A}+1}) + A(\cancel{1+B}) \\
&= CD + A
\end{aligned}$$

$$\begin{aligned}
\text{(c)} \quad & (A+C+D)(A+C+\bar{D})(A+\bar{C}+D)(A+\bar{B}) \\
&= [(A+C)(A+C) + (A+C)\bar{D} + (A+C)D + \cancel{D\bar{D}}] (A+\bar{C}+D)(A+\bar{B}) \\
&= (A+C) \underbrace{[(A+C) + \bar{D} + D]}_1 (A+\bar{C}+D)(A+\bar{B}) \\
&= (A+C)(A+\bar{C}+D)(A+\bar{B}) \\
&= (AA + A\bar{C} + AD + CA + \cancel{C\bar{C}} + CD)(A+\bar{B}) \\
&= [A \underbrace{[A + D + \bar{C} + C]}_1 + CD](A+\bar{B}) \\
&= (A + CD)(A+\bar{B}) = A + \bar{B}CD
\end{aligned}$$

Q.10

(a)

| A | B | C | ABC | $\overline{A}\overline{B}C$ | $\overline{A}B\overline{C}$ | $A\overline{B}\overline{C}$ | $\overline{A}\overline{B}\overline{C}$ | OUTPUT |
|---|---|---|-----|-----------------------------|-----------------------------|-----------------------------|--|--------|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 |
| 0 | 0 | 1 | 0 | 1 | 0 | 0 | 0 | 1 |
| 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 0 | 0 | 1 | 0 | 0 | 1 |
| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1 | 1 | 0 | 0 | 0 | 0 | 1 | 0 | 1 |
| 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 1 |

| A | B | C | $B(A+C)$ | $\overline{A}\overline{B}$ | OUTPUT |
|---|---|---|----------|----------------------------|--------|
| 0 | 0 | 0 | 0 | 1 | 1 |
| 0 | 0 | 1 | 0 | 1 | 1 |
| 0 | 1 | 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 1 | 1 ← ? | 1 |
| 1 | 0 | 0 | 0 | 0 | 0 |
| 1 | 0 | 1 | 0 | 0 | 0 |
| 1 | 1 | 0 | 1 | 0 | 1 |
| 1 | 1 | 1 | 1 | 0 | 1 |

thus $B(A+C) + \overline{A}\overline{B}$

$= ABC + \overline{A}\overline{B}C + \overline{A}B\overline{C} + A\overline{B}\overline{C} + \overline{A}\overline{B}\overline{C}$

(b)

| ABCD | $\overline{CD+A}$ | A | CD | AB | Z | CD | A | Z* |
|------|-------------------|---|----|----|---|----|---|----|
| 0000 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0001 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0010 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0011 | 1 | 0 | 1 | 0 | 1 | 1 | 0 | 1 |
| 0100 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0101 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0110 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0111 | 1 | 0 | 1 | 0 | 1 | 1 | 0 | 1 |
| 1000 | 0 | 1 | 0 | 0 | 1 | 0 | 1 | 1 |
| 1001 | 0 | 1 | 0 | 0 | 1 | 0 | 1 | 1 |
| 1010 | 0 | 1 | 0 | 0 | 1 | 0 | 1 | 1 |
| 1011 | 0 | 1 | 1 | 0 | 1 | 1 | 1 | 1 |
| 1100 | 0 | 1 | 0 | 1 | 1 | 0 | 1 | 1 |
| 1101 | 0 | 1 | 0 | 1 | 1 | 0 | 1 | 1 |
| 1110 | 0 | 1 | 0 | 1 | 1 | 0 | 1 | 1 |
| 1111 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |

$$Z = \overline{CD+A} + A + CD + AB$$

$$Z^* = CD + A$$

By the truth table, $Z = Z^*$

(c)

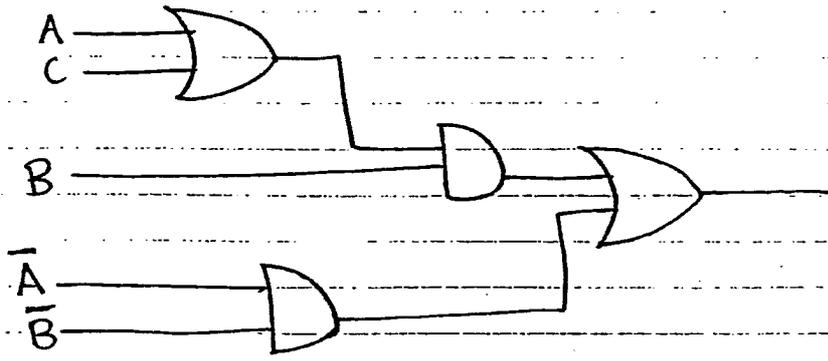
| ABCD | A+C+D | A+C+ \overline{D} | A+C+D | A+B | Z | A | \overline{BCD} | Z* |
|------|-------|---------------------|-------|-----|---|---|------------------|----|
| 0000 | 0 | 1 | 1 | 1 | 0 | 0 | 0 | 0 |
| 0001 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 0 |
| 0010 | 1 | 1 | 0 | 1 | 0 | 0 | 0 | 0 |
| 0011 | 1 | 1 | 1 | 1 | 1 | 0 | 1 | 1 |
| 0100 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 |
| 0101 | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| 0110 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0111 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 |
| 1000 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1001 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1010 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1011 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1100 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1101 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1110 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1111 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |

$$Z = (A+C+D)(A+C+\overline{D})(A+C+D)(A+B), \quad Z^* = A + \overline{BCD}$$

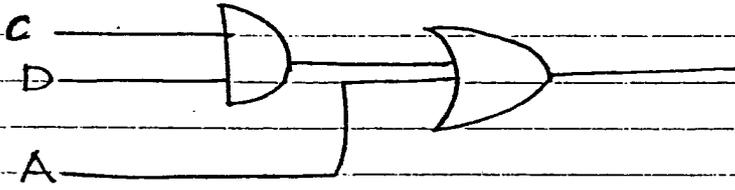
Again $Z = Z^*$

Q11

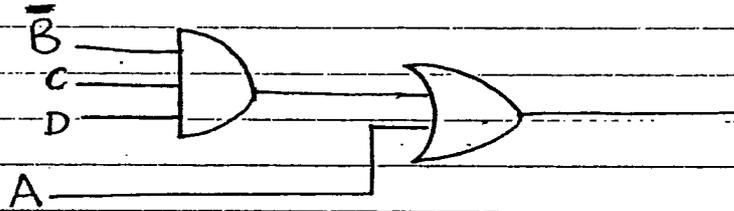
a)



b)



a)



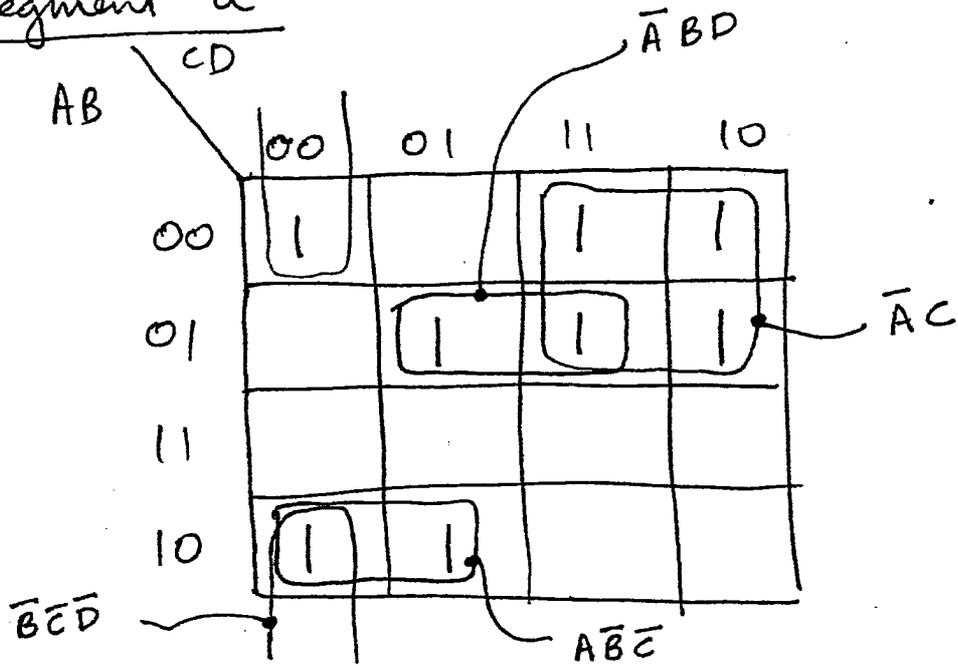
(6)

| | BINARY-CODED-DECIMAL | | | | SEGMENT SELECTED | | | | | | |
|----|----------------------|---|---|---|------------------|---|---|---|---|---|---|
| | A | B | C | D | a | b | c | d | e | f | g |
| 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 0 |
| 1 | 0 | 0 | 0 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 0 |
| 2 | 0 | 0 | 1 | 0 | 1 | 1 | 0 | 1 | 1 | 0 | 1 |
| 3 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 1 |
| 4 | 0 | 1 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 1 |
| 5 | 0 | 1 | 0 | 1 | 1 | 0 | 1 | 1 | 0 | 1 | 1 |
| 6 | 0 | 1 | 1 | 0 | 1 | 0 | 1 | 1 | 1 | 1 | 1 |
| 7 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 |
| 8 | 1 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 9 | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 0 | 1 | 1 |
| 10 | 1 | 0 | 1 | 0 | | | | | | | |
| 11 | 1 | 0 | 1 | 1 | | | | | | | |
| 12 | 1 | 1 | 0 | 0 | | | | | | | |
| 13 | 1 | 1 | 0 | 1 | | | | | | | |
| 14 | 1 | 1 | 1 | 0 | | | | | | | |
| 15 | 1 | 1 | 1 | 1 | | | | | | | |

Note: Invalid input combinations (i.e., for 10, 11, 12, 13, 14, and 15) have been made equal to "0" for a blank display, rather than allowing them to be "don't care" states.

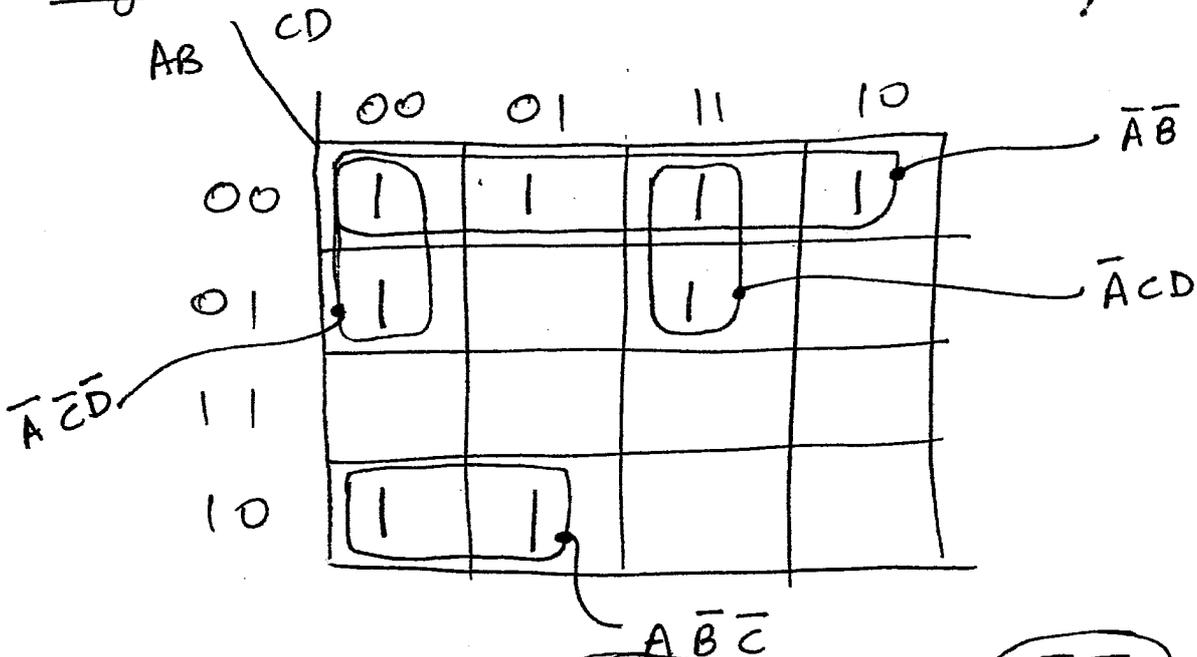
Note: product terms shared between more than one output have been circled

segment a



$$a = \bar{A}C + \bar{A}BD + \bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}$$

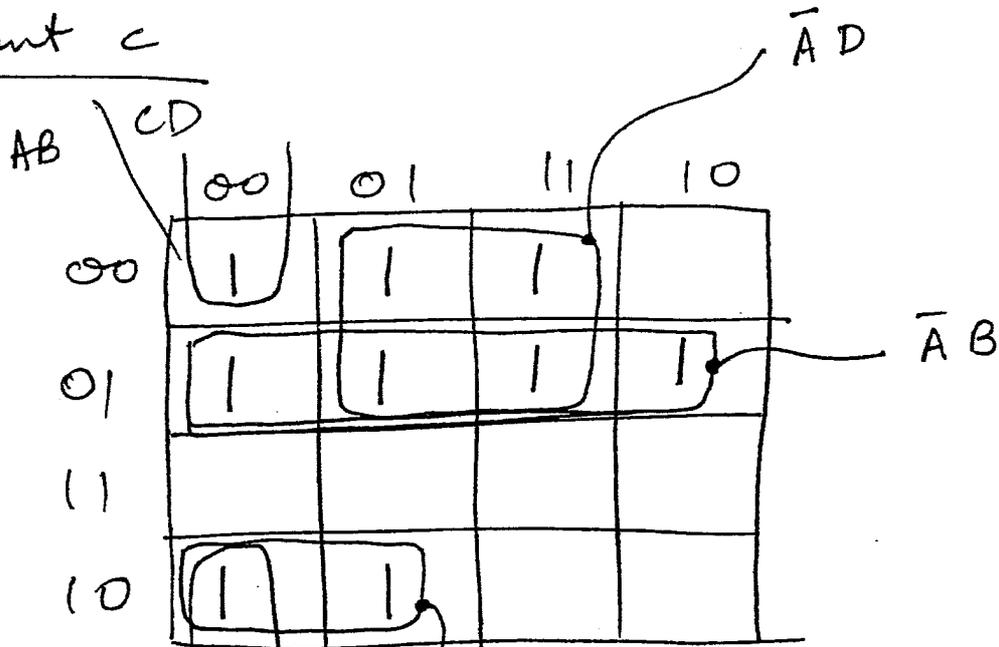
segment b



$$b = \bar{A}\bar{B} + \bar{A}\bar{C}\bar{D} + \bar{A}CD + \bar{A}\bar{B}\bar{C}$$

Note: rather than form the larger group using minterms 0, 1, 8, 9 to give $\bar{B}\bar{C}$ leave it as $\bar{A}\bar{B}\bar{C}$ (ie minterms 8, 9) since these two occur quite often in other Karnaugh maps

segment c



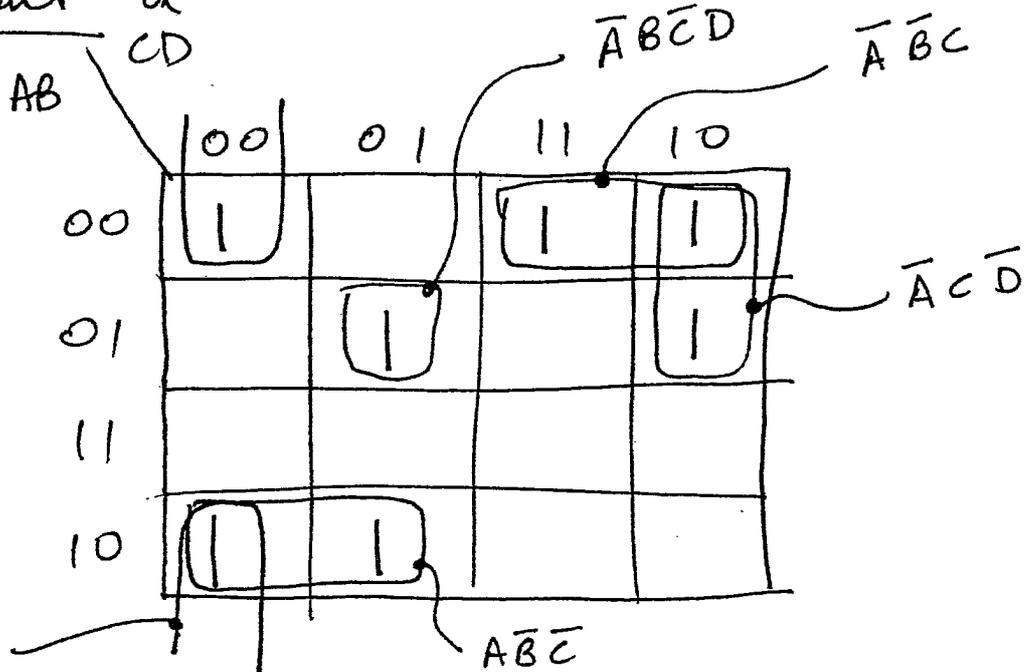
$\overline{B\overline{C}\overline{D}}$

$A\overline{B}\overline{C}$

$$c = \overline{A}B + \overline{A}D + \overline{B\overline{C}\overline{D}} + \overline{A\overline{B}\overline{C}}$$

Once again rather than form larger groups (minterms 0,1,4,5 and minterms 0,1,8,9) we leave it as $\overline{A\overline{B}\overline{C}}$ and $\overline{B\overline{C}\overline{D}}$ since we already need to form these product terms to implement segment "a".

segment d

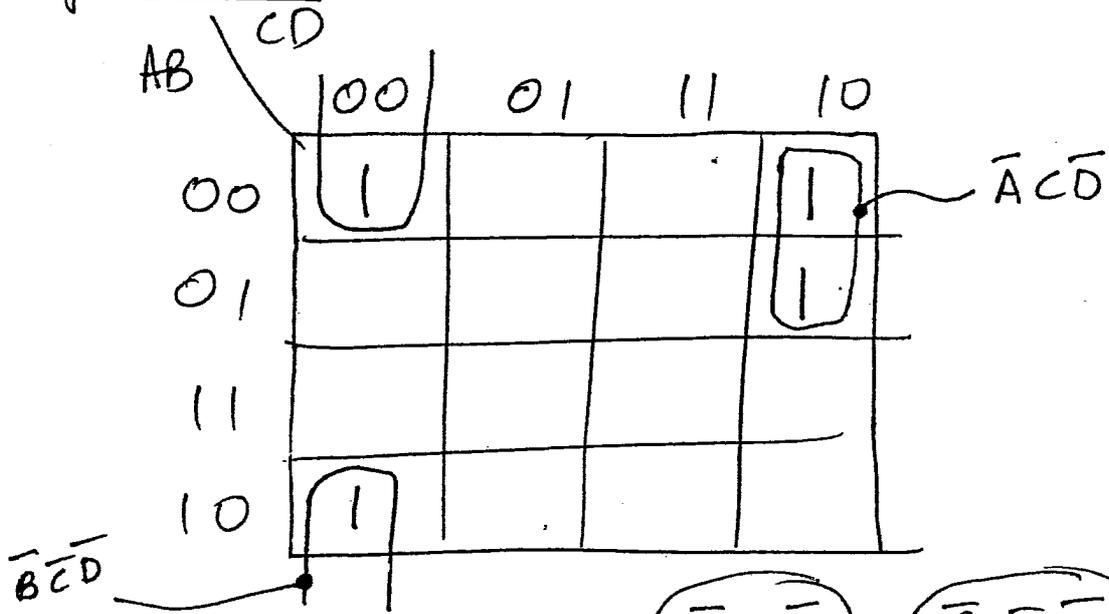


$\overline{B\overline{C}\overline{D}}$

$A\overline{B}\overline{C}$

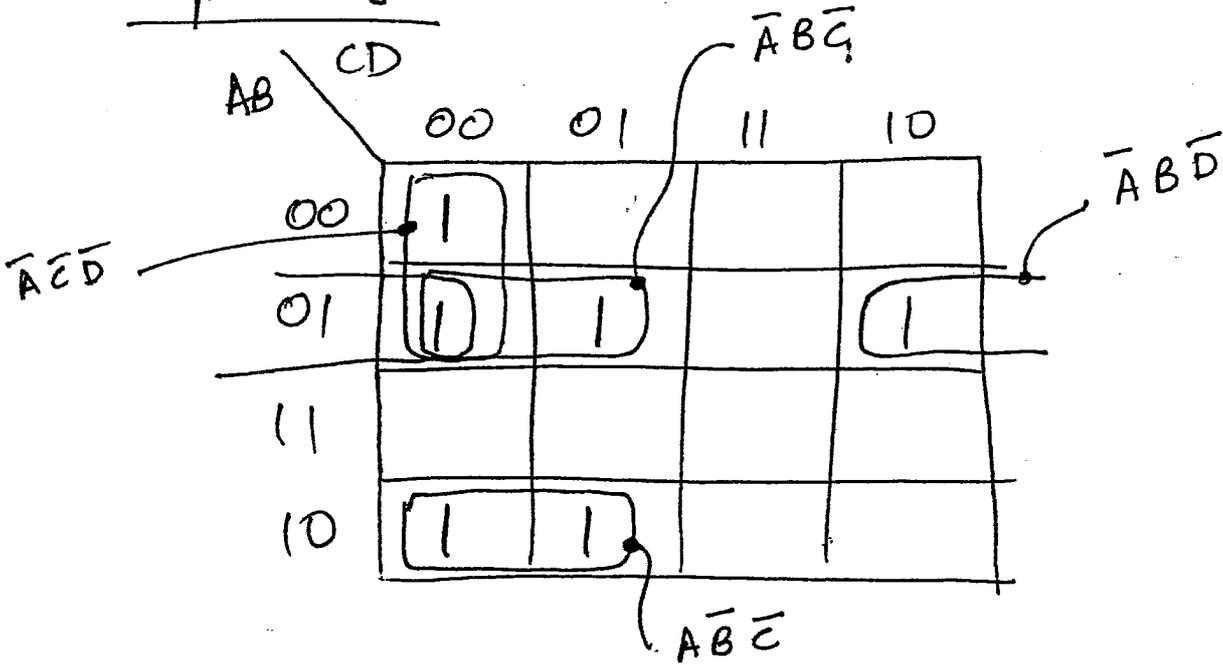
$$d = \overline{A\overline{C}\overline{D}} + \overline{A\overline{B}\overline{C}} + \overline{B\overline{C}\overline{D}} + \overline{A\overline{B}\overline{C}} + \overline{A\overline{B}\overline{C}D}$$

segment e



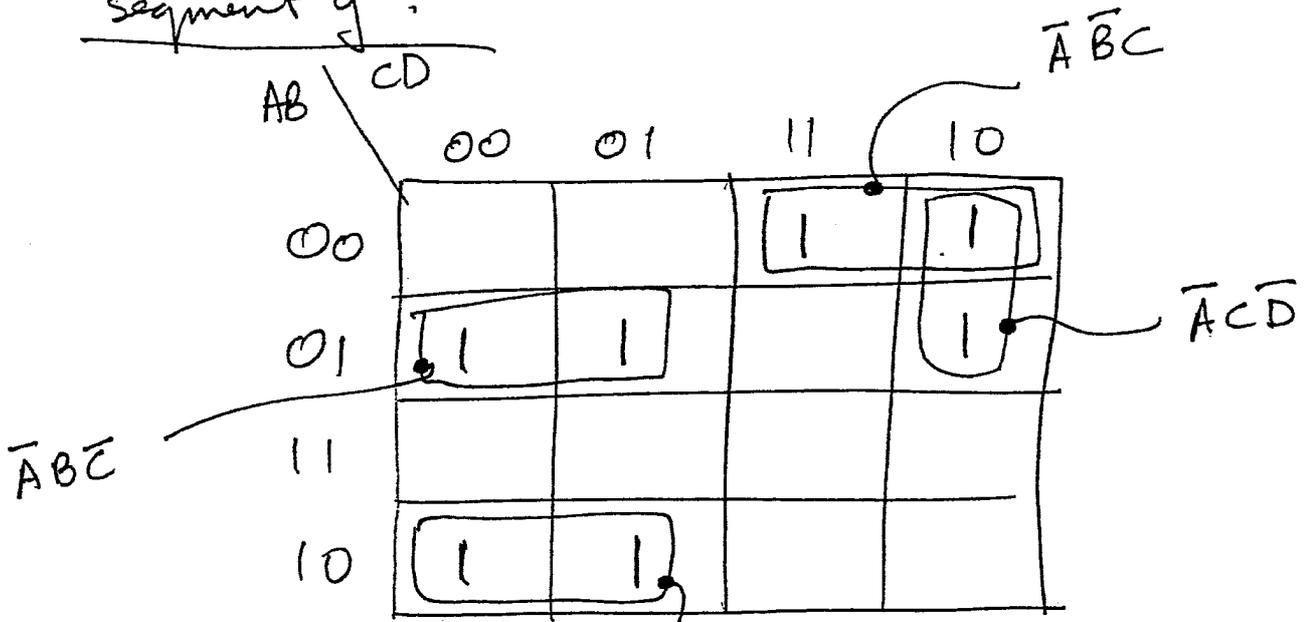
$$e = \bar{A}\bar{C}\bar{D} + \bar{B}\bar{C}\bar{D}$$

segment f



$$f = \bar{A}\bar{C}\bar{D} + \bar{A}B\bar{C} + \bar{A}B\bar{D} + \bar{A}B\bar{C}$$

segment g .



$$g = \overline{A}C\overline{D} + \overline{A}\overline{B}C + \overline{A}B\overline{C} + \overline{A}B\overline{C}$$

Decimal Display Circuit

